

Exclusive Semileptonic B Decays and $|V_{ub}|$: Experimental

4th Flavor and CP Violation Conference
Vancouver, BC
9th - 12th April 2006

Kevin Varvell
University of Sydney



Significance of $|V_{ub}|$ Measurement

§ Precision measurement of SM parameter, size not theoretically predicted

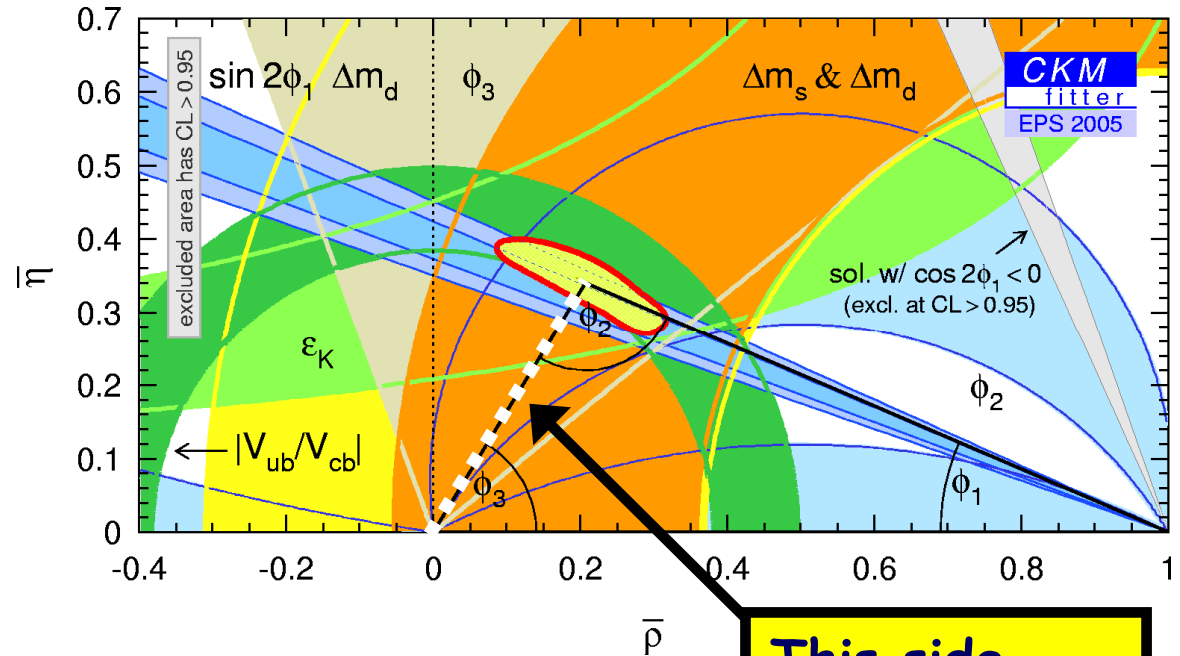
§ Constrain one side of the Unitarity Triangle

§ Test consistency of SM picture, particularly between $|V_{ub}|/|V_{cb}|$ and $\sin 2\phi_1$ ($\sin 2\beta$)

§ Current precision

- § $\sin 2\phi_1 \sim 4\%$
- § $|V_{cb}| \sim 2\%$ (one recent update mentioned here)
- § $|V_{ub}| \sim 7\%$ inclusive (talk this afternoon, E. Barberio)
- § $>10\%$ exclusive (main subject of this talk)

§ Aim is for $< 5\%$ precision for $|V_{ub}|_{\text{excl}}$, compare with $|V_{ub}|_{\text{incl}}$

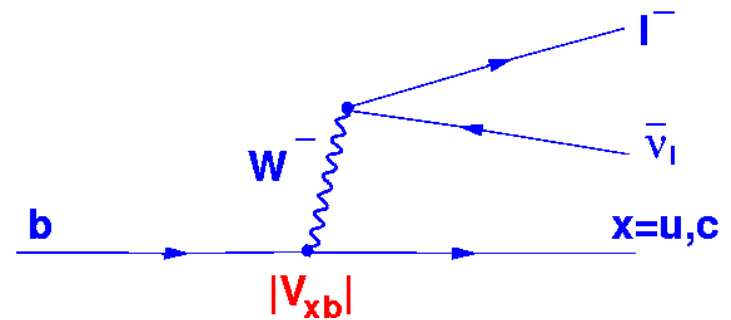


This side determined By $|V_{ub}|/|V_{cb}|$

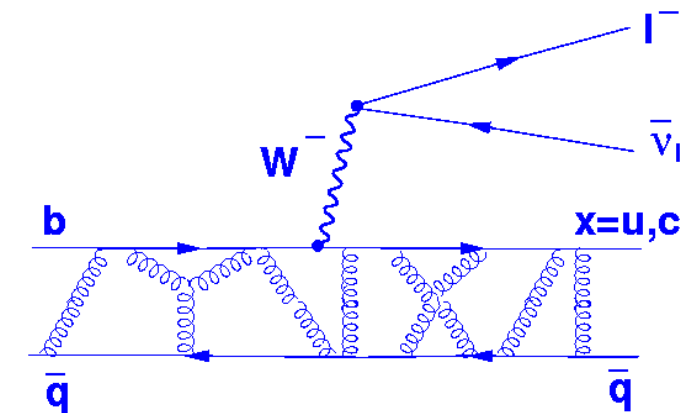
From Exclusive Semileptonic B decay to $|V_{ub}|$

Measurements made in $e^+e^- \rightarrow Y(4S) \rightarrow B\bar{B}$

Ideally want to measure rate of tree level process $\Gamma(b \rightarrow x \ell \nu)$



Complicated by strong interaction effects - **form factors** needed



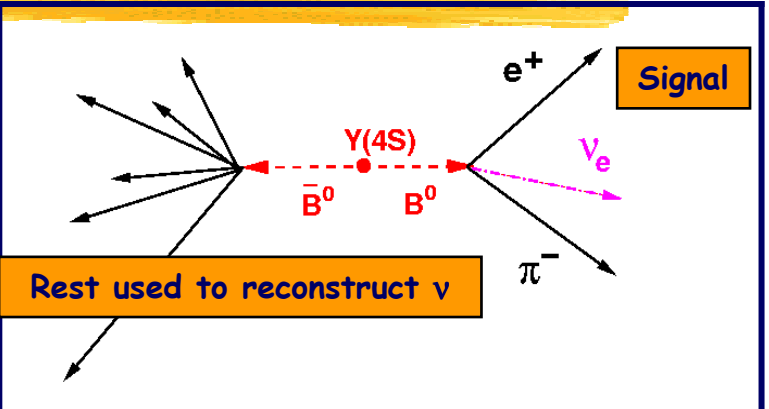
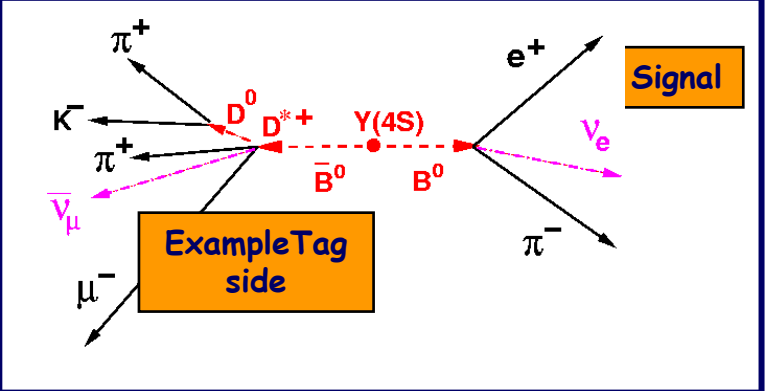
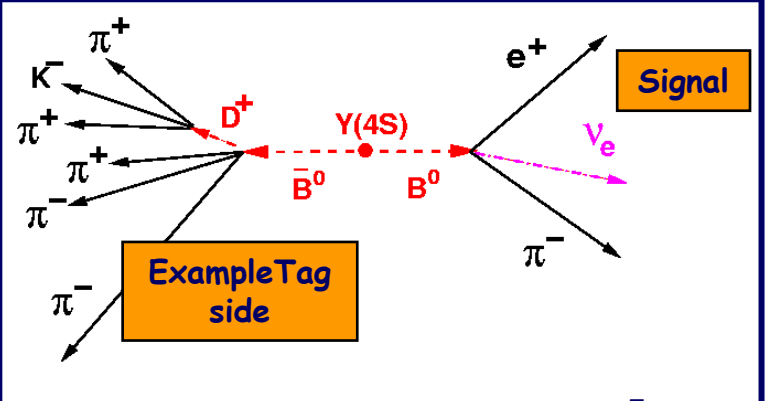
Channel $B \rightarrow \pi \ell \nu$ is the most promising for $|V_{ub}|$
 - one dominant form factor $f_+(q^2)$
 q^2 shape and normalization needed

$$\frac{d\Gamma(B \rightarrow \pi \ell \nu)}{dq^2} = \frac{G_F^2}{2\pi^3} |V_{ub}|^2 p_\pi^3 |f_+(q^2)|^2$$

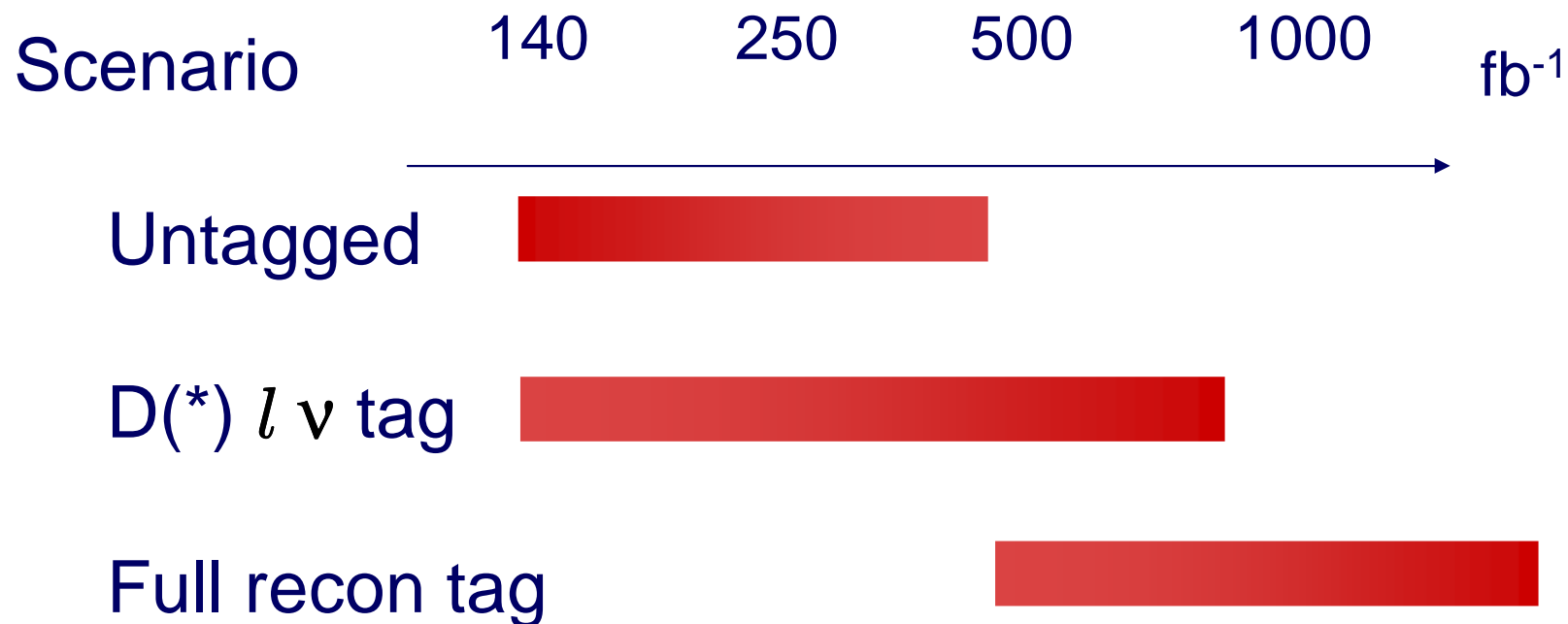
Determining the Form Factor $f_+(q^2)$

- § Earlier predictions made with quark models, e.g. ISGW2
- § Lattice QCD
 - § makes predictions at high q^2 ($q^2 > \sim 16 \text{ GeV}^2$)
 - § unquenched calculations have become available in recent times
 - § e.g. HPQCD [hep-lat-0601201](#)
FNAL [hep-lat-0409116](#)
- § Light Cone Sum Rules
 - § makes predictions at low q^2 ($q^2 < \sim 14 \text{ GeV}^2$)
 - § e.g. Ball & Zwicky [PRD 71 \(2005\) 014015](#)
- § Parametrization has traditionally been used to extend LQCD or LCSR to full q^2 range
- § FF normalization main issue when extracting $|V_{ub}|$
- § How much theory input needed for $|V_{ub}|$ measurement? [hep-ph/0509090](#)
(R. Hill talk)

Approaches to Measuring $B(B \rightarrow \pi \ell \nu)$

<p>Untagged</p> <ul style="list-style-type: none"> § initial 4-momentum known § missing 4-momentum = ν § Reconstruct $B \rightarrow \pi \ell \nu$ using m_B (beam-constrained) and $\Delta E = E_B - E_{\text{beam}}$ 	<p>Pros</p> <ul style="list-style-type: none"> § High efficiency <p>Cons</p> <ul style="list-style-type: none"> § ν resolution problematic § Rel. high backgrounds (rel. low purity) 	
<p>Semileptonic (SL) Tag</p> <ul style="list-style-type: none"> § One B reconstructed in a selection of $D^{(*)} \ell \nu$ modes § Two missing ν in event Use kinematic constraints 	<p>Pros</p> <ul style="list-style-type: none"> § Lower backgrounds (higher purity) <p>Cons</p> <ul style="list-style-type: none"> § Rel. low efficiency 	
<p>Full Recon Tag</p> <ul style="list-style-type: none"> § One B reconstructed completely in known $b \rightarrow c$ mode. Many modes used. 	<p>Pros</p> <ul style="list-style-type: none"> § Very good ν resolution § Very low backgrounds <p>Cons</p> <ul style="list-style-type: none"> § Very low efficiency 	

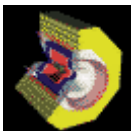
Range of Applicability of Methods



- Boundaries indicative only
- Full recon tag will ultimately become method of choice.

Currently

Belle $\mathcal{L}_{\text{int}} \sim 500 \text{ fb}^{-1}$
BaBar $\mathcal{L}_{\text{int}} \sim 300 \text{ fb}^{-1}$



CLEO Untagged $B \rightarrow \pi \ell \nu$

Phys. Rev. D 68 (2003) 072003

(9.7M $B\bar{B}$)

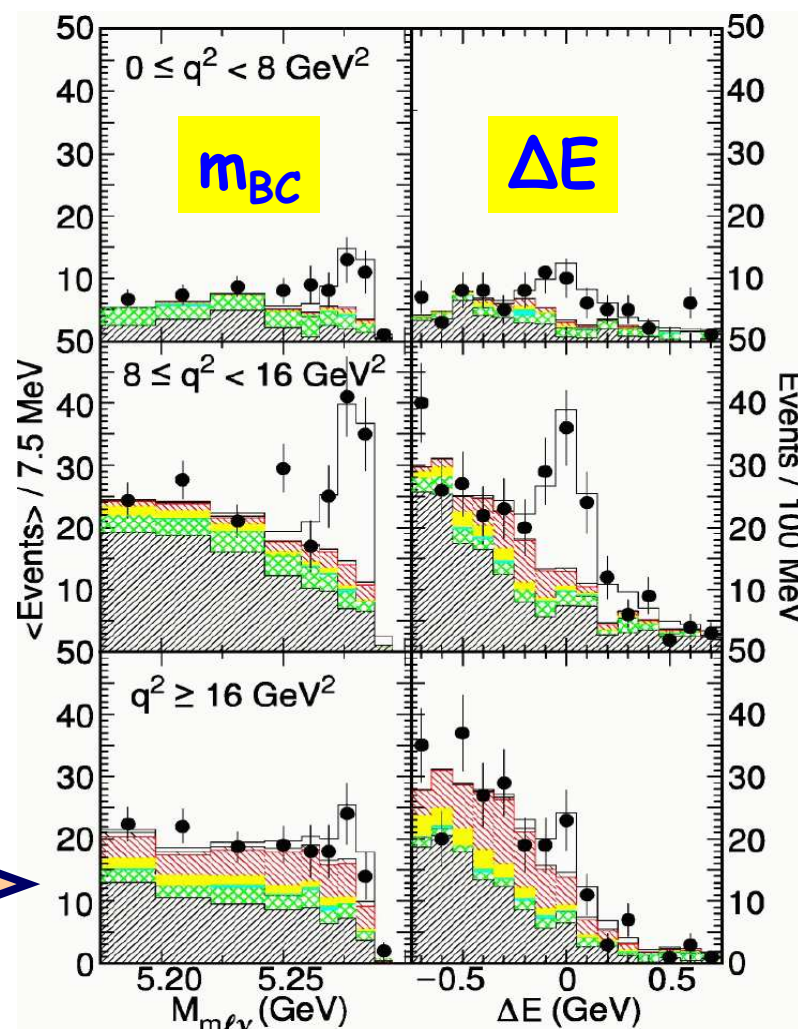
§ Search (and fit for yields) across a number of exclusive $X_\ell \ell \nu$ modes

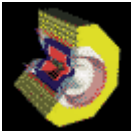
$\pi^+, \pi^0, \rho^+, \rho^0, \omega, \eta$

§ Isospin constraints imposed in fit

§ Extract partial BF in 3 q^2 bins for π^+ and ρ^+

π^- result \rightarrow





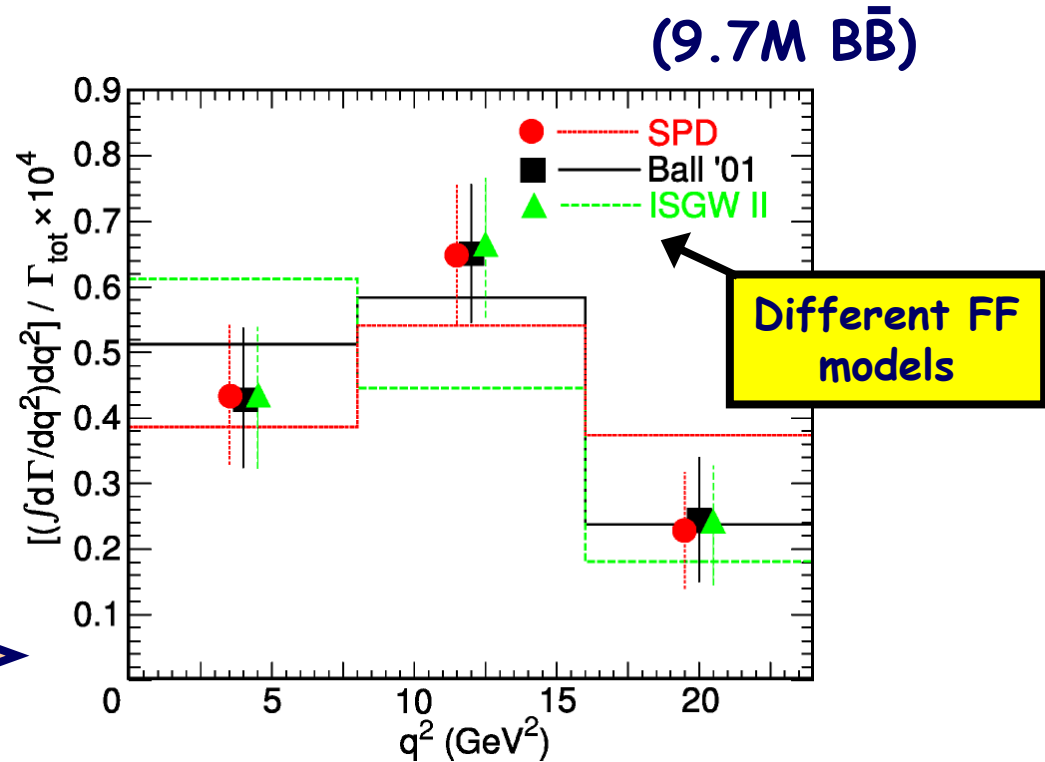
CLEO Untagged $B \rightarrow \pi \ell \nu$ (cont.)

Phys. Rev. D 68 (2003) 072003

FF models enter extraction of BF through

- Signal efficiency from MC
- $b \rightarrow u$ crossfeed and $b \rightarrow c$ background modelling in MC

π^- result \rightarrow



$$B(B^0 \rightarrow \pi^- \ell^+ \nu) = (1.33 \pm 0.18 \pm 0.11 \pm 0.01 \pm 0.07) \times 10^{-4}$$

stat
syst
FF sig
FF crossfeed

$$|V_{ub}| = (3.17 \pm 0.17 \pm 0.16 \pm 0.53 \pm 0.03) \times 10^{-3}$$

stat
syst
theo
FF shape ρ

(π and ρ mode combined)
 LCSR + LQCD (unq)

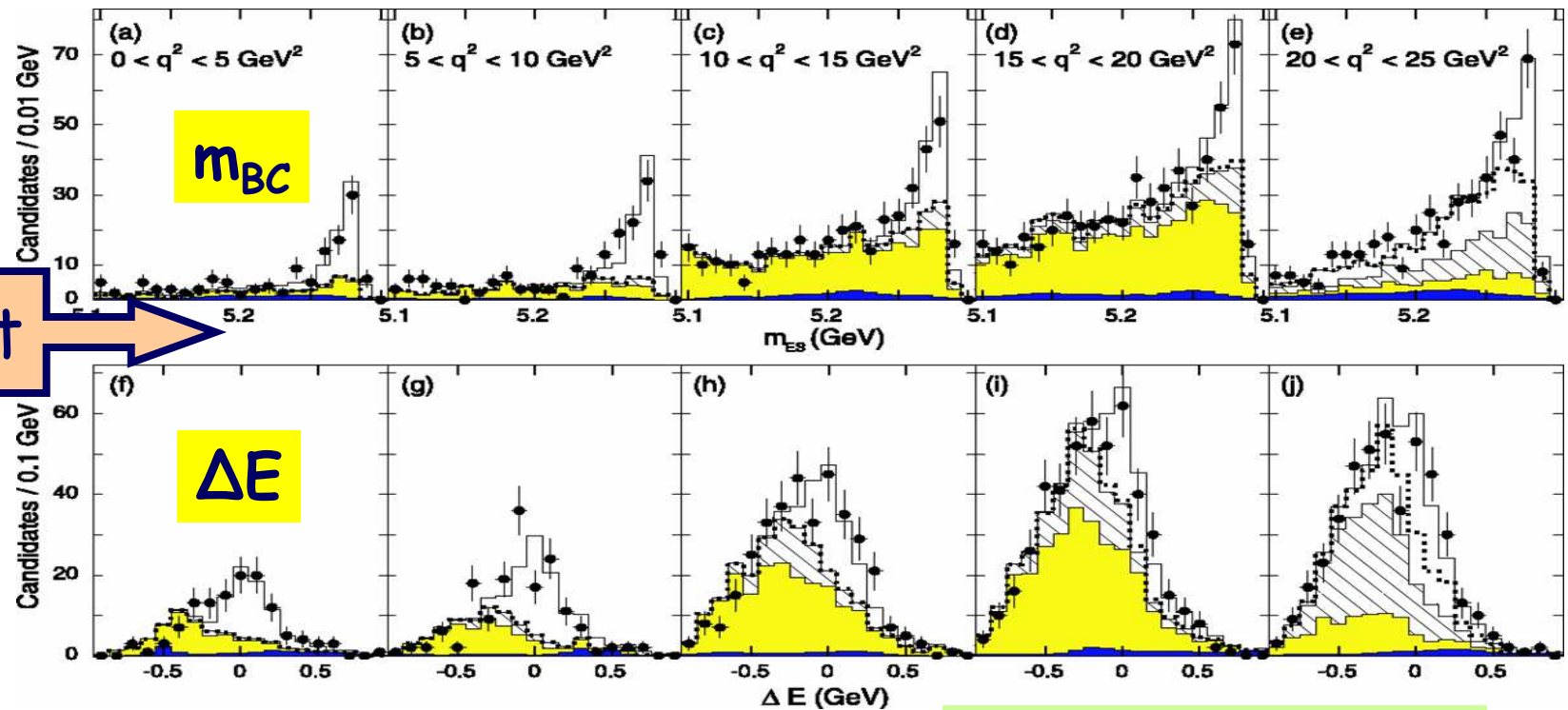


BaBar Untagged $B^0 \rightarrow \pi^- \ell^+ \nu$

Phys. Rev. D72 (2005) 051102

79fb^{-1} (86M $B\bar{B}$)

Simultaneous extraction of modes $\pi^+, \pi^0, \rho^+, \rho^0$



Yield 396 $\pi^-\ell\nu$, 137 $\pi^0\ell\nu$



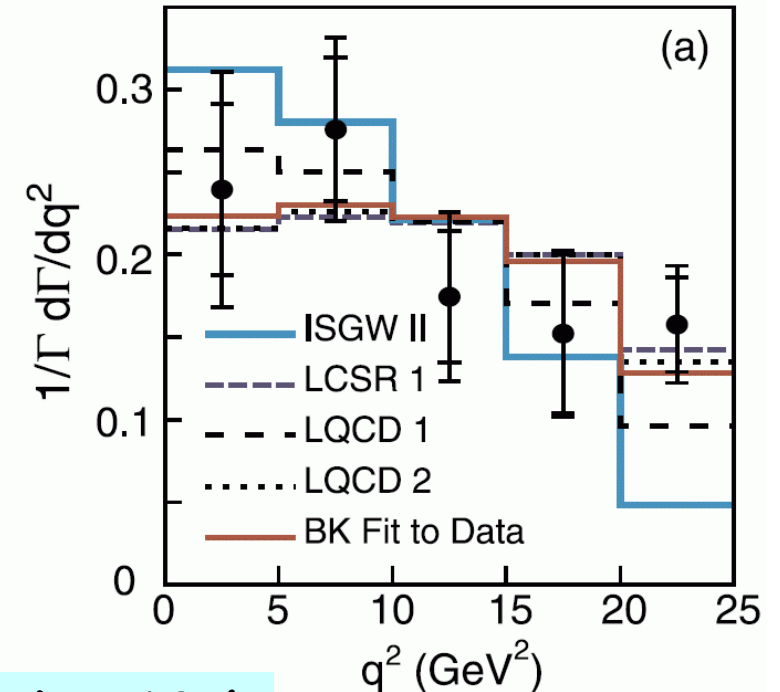
BaBar Untagged $B^0 \rightarrow \pi^- \ell^+ \nu$ (cont)

Phys. Rev. D72 (2005) 051102

79fb⁻¹ (86M $B\bar{B}$)

- § Isospin constraints imposed
- § Extract partial BF in
 - § 5 q^2 bins π
 - § 3 q^2 bins ρ
- § "Marginal" agreement with ISGW2

π^- result \rightarrow



$$B(B^0 \rightarrow \pi^- \ell^+ \nu) = (1.38 \pm 0.10 \pm 0.16 \pm 0.08) \times 10^{-4}$$

stat syst FF shape

$$|V_{ub}| = (3.82 \pm 0.14 \pm 0.22 \pm 0.11 \begin{matrix} +0.88 \\ -0.52 \end{matrix}) \times 10^{-3}$$

stat syst FF shape FF norm

FNAL LQCD



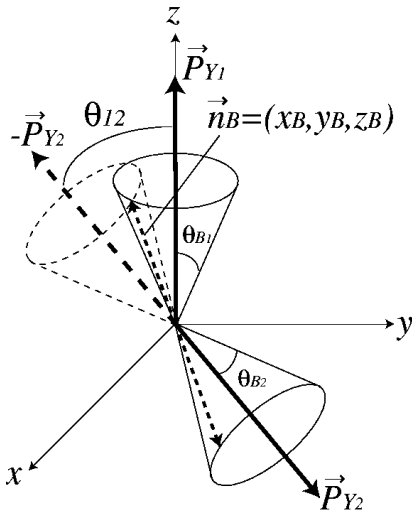
Belle SL Tag $B \rightarrow \pi \ell^+ \nu$

hep-ex/0604024

Submitted to PLB

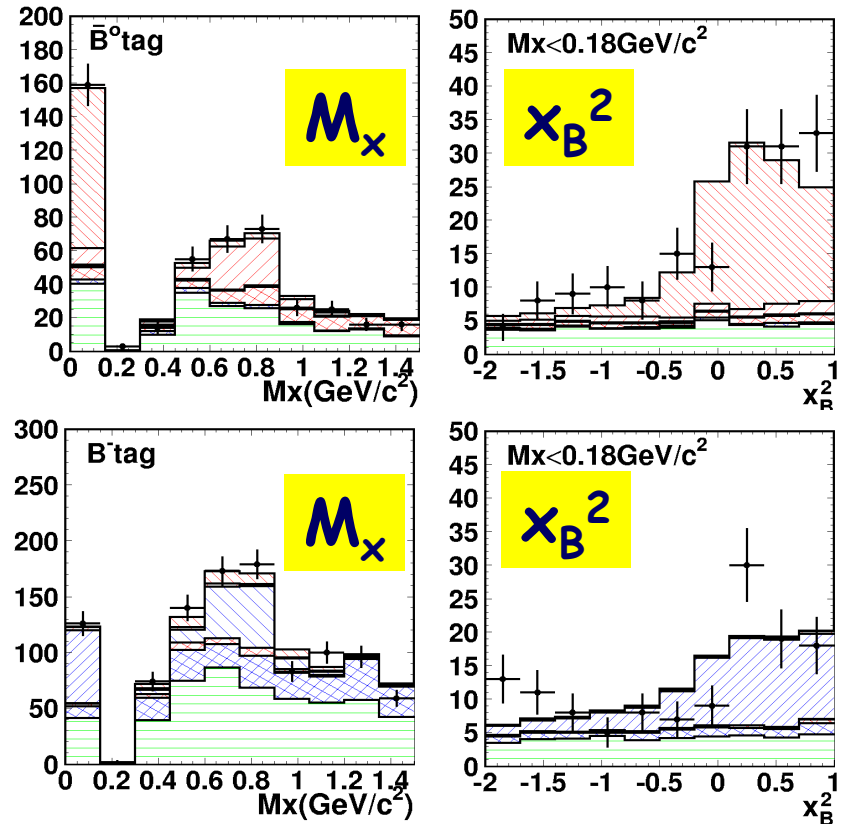
253fb⁻¹ (275M B \bar{B})

§ Simultaneous extraction of modes $\pi^+, \pi^0, \rho^+, \rho^0$



$$x_B^2 = 1 - \frac{1}{\sin^2 \theta_{12}} \cdot (\cos^2 \theta_{B_1} + \cos^2 \theta_{B_2} - 2 \cos \theta_{B_1} \cos \theta_{B_2} \cos \theta_{12})$$

§ x_B^2 must lie in range [0,1] for signal events



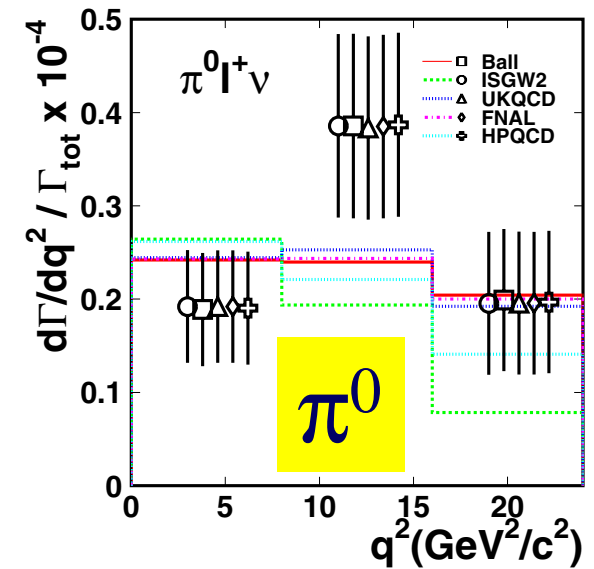
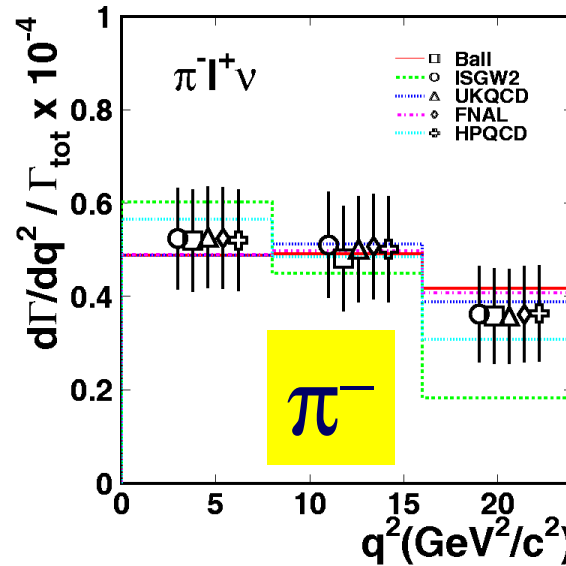
Yield 156 $\pi \ell \nu$, 69 $\pi^0 \ell \nu$



Belle SL Tag $B \rightarrow \pi \ell^+ \nu$ (cont)

hep-ex/0604024

§ Extract partial BF in 3 q^2 bins



$$B(B^0 \rightarrow \pi^- \ell^+ \nu) = (1.38 \pm 0.19 \pm 0.14 \pm 0.03) \times 10^{-4}$$

stat syst FF shape

$$B(B^+ \rightarrow \pi^0 \ell^+ \nu) = (0.77 \pm 0.14 \pm 0.09 \pm 0.00) \times 10^{-4}$$

stat syst FF shape

$$|V_{ub}| = (3.60 \pm 0.41 \pm 0.20 \pm 0.62 \pm 0.41) \times 10^{-3}$$

stat syst theo

$\pi^+ + \pi^0, q^2 \geq 16 \text{ GeV}^2, \text{ FNAL}$

$$|V_{ub}| = (4.03 \pm 0.46 \pm 0.22 \pm 0.59 \pm 0.41) \times 10^{-3}$$

stat syst theo

$\pi^+ + \pi^0, q^2 \geq 16 \text{ GeV}^2, \text{ HPQCD}$

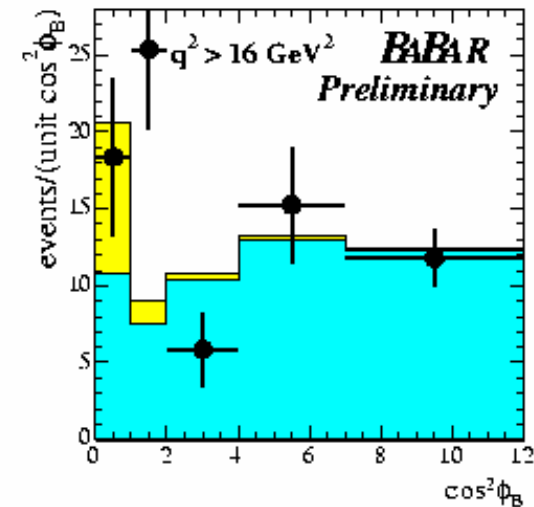
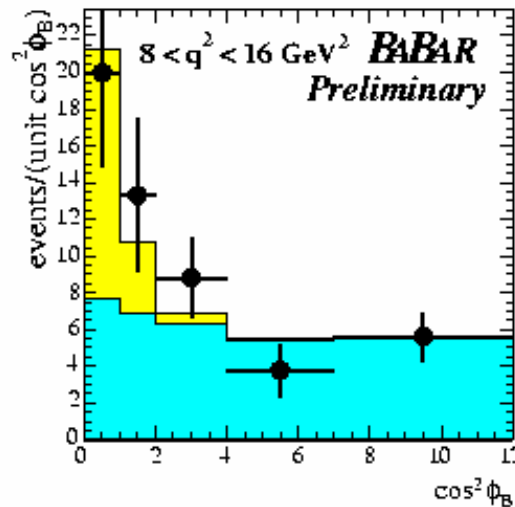
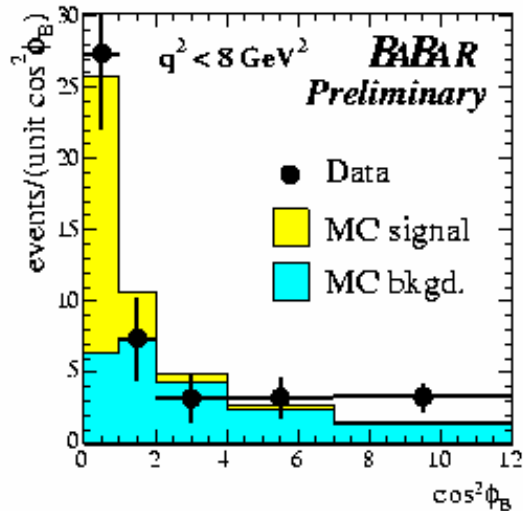
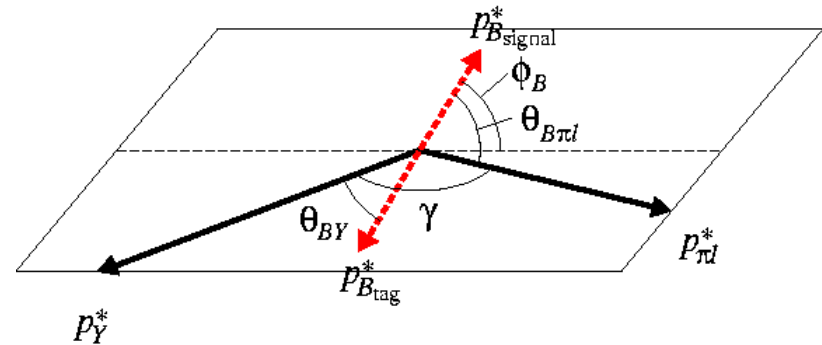


BaBar SL Tag $B^0 \rightarrow \pi^- \ell^+ \nu$

hep-ex/0506064

211fb⁻¹ (232M $B\bar{B}$)

- Single mode π^- studied
- $\cos^2\phi_B \in [0,1]$ for signal events



Yield 61 $\pi\ell\nu$

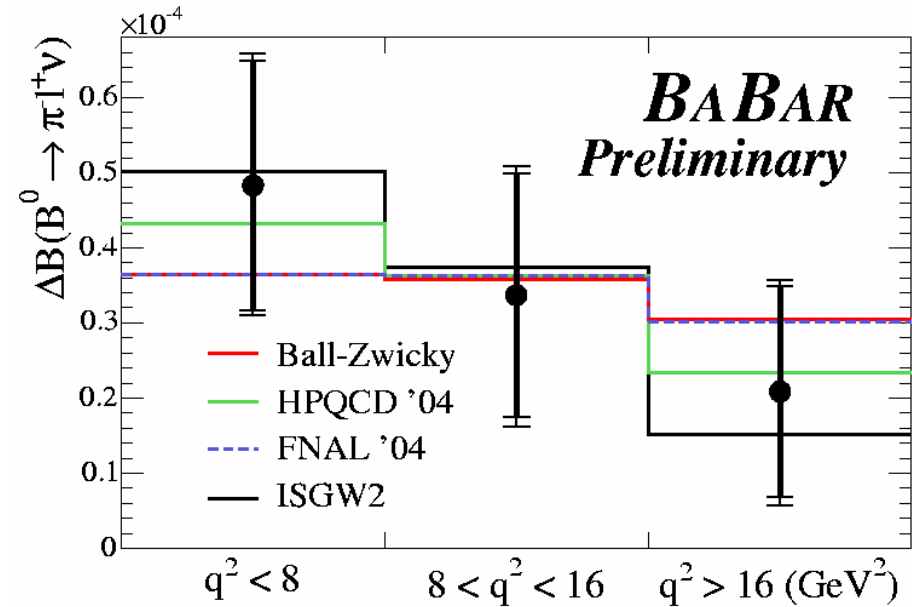


BaBar SL Tag $B^0 \rightarrow \pi^- \ell^+ \nu$ (cont)

hep-ex/0506064

211fb⁻¹ (232M $B\bar{B}$)

Extract partial BF in 3 q^2 bins



$$B(B^0 \rightarrow \pi^- \ell^+ \nu) = (1.03 \pm 0.25_{\text{stat}} \pm 0.13_{\text{syst}}) \times 10^{-4}$$

$$|V_{ub}| = (3.3 \pm 0.4_{\text{stat}} \pm 0.2_{\text{syst}} \pm 0.8_{\text{FF norm}} \pm 0.4_{\text{FF norm}}) \times 10^{-3}$$

HPQCD04



BaBar SL Tag $B^+ \rightarrow \pi^0 \ell^+ \nu$

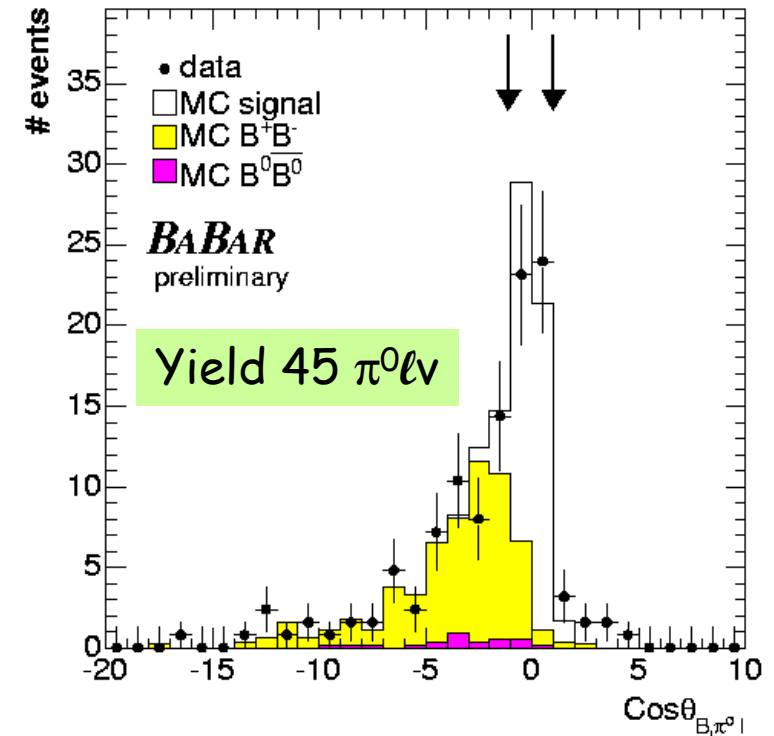
hep-ex/0506065

81fb⁻¹ (88M $B\bar{B}$)

§ Single mode π^0 studied

$$\cos \theta_{B\pi^0\ell} = \frac{2E_B^* E_{\pi^0\ell}^* - m_B^2 - m_{\pi^0\ell}^2}{2p_B^* p_{\pi^0\ell}^*}$$

§ $\cos \theta_{B\pi^0\ell} \in [-1, 1]$ for signal events



$$\mathcal{B}(B^+ \rightarrow \pi^0 \ell^+ \nu) = (1.80 \pm 0.37_{\text{stat}} \pm 0.23_{\text{syst}}) \times 10^{-4}$$

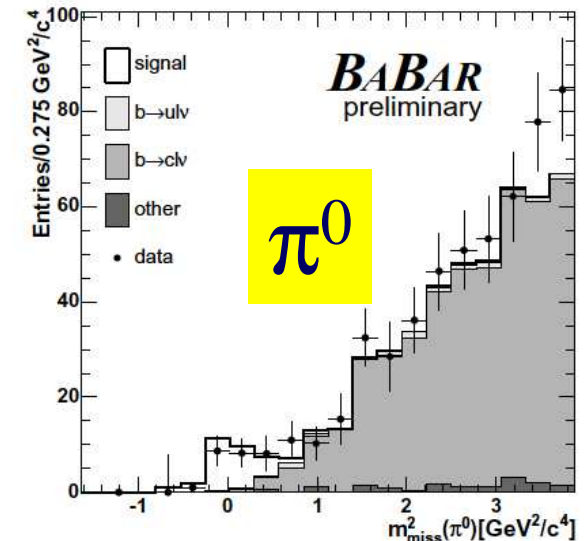
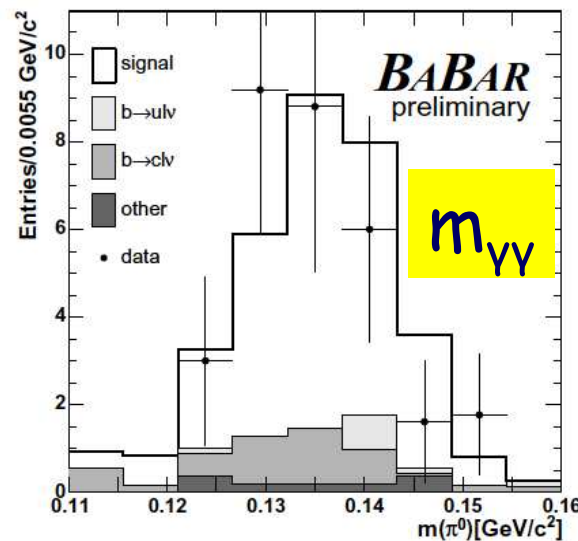
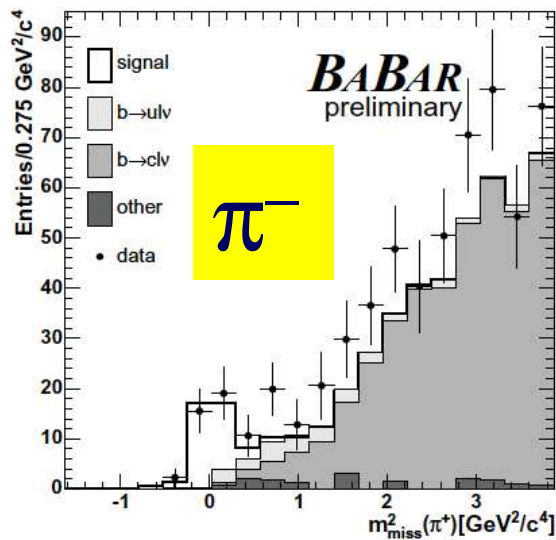


BaBar Full Recon Tag $B \rightarrow \pi \ell^+ \nu$

hep-ex/0507085

211fb⁻¹ (233M B \bar{B})

- Tag : Fully reconstructed $B \rightarrow D$ decays ("Breco" tag)
Select using ΔE , m_{ES} (beam constrained B candidate mass)
- m_{miss}^2 distribution : peaks at zero for signal (single missing neutrino)



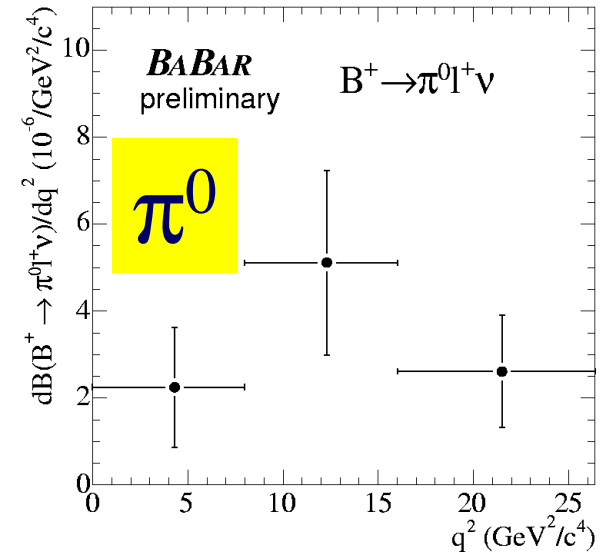
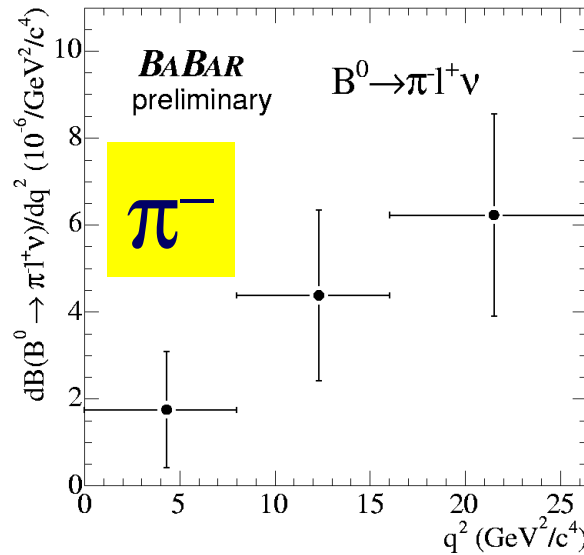
Yield 36 $\pi\ell\nu$, 34 $\pi^0\ell\nu$



BaBar Full Recon Tag $B \rightarrow \pi \ell^+ \nu$

hep-ex/0507085

Extract partial BF in 3 q^2 bins



$$B(B^0 \rightarrow \pi^- \ell^+ \nu) = (1.14 \pm 0.27_{\text{stat}} \pm 0.17_{\text{syst}}) \times 10^{-4}$$

$$B(B^+ \rightarrow \pi^0 \ell^+ \nu) = (0.86 \pm 0.22_{\text{stat}} \pm 0.11_{\text{syst}}) \times 10^{-4}$$

$$B(B \rightarrow \pi \ell^+ \nu) = (1.28 \pm 0.23_{\text{stat}} \pm 0.16_{\text{syst}}) \times 10^{-4}$$

Combined $\pi^+ + \pi^0$

$$|V_{ub}| = (3.7 \pm 0.3_{\text{stat}} \pm 0.2_{\text{syst}} \pm 0.8_{\text{FF norm}} \mp 0.5_{\text{FF norm}}) \times 10^{-3}$$

$\pi^+ + \pi^0$, HPQCD

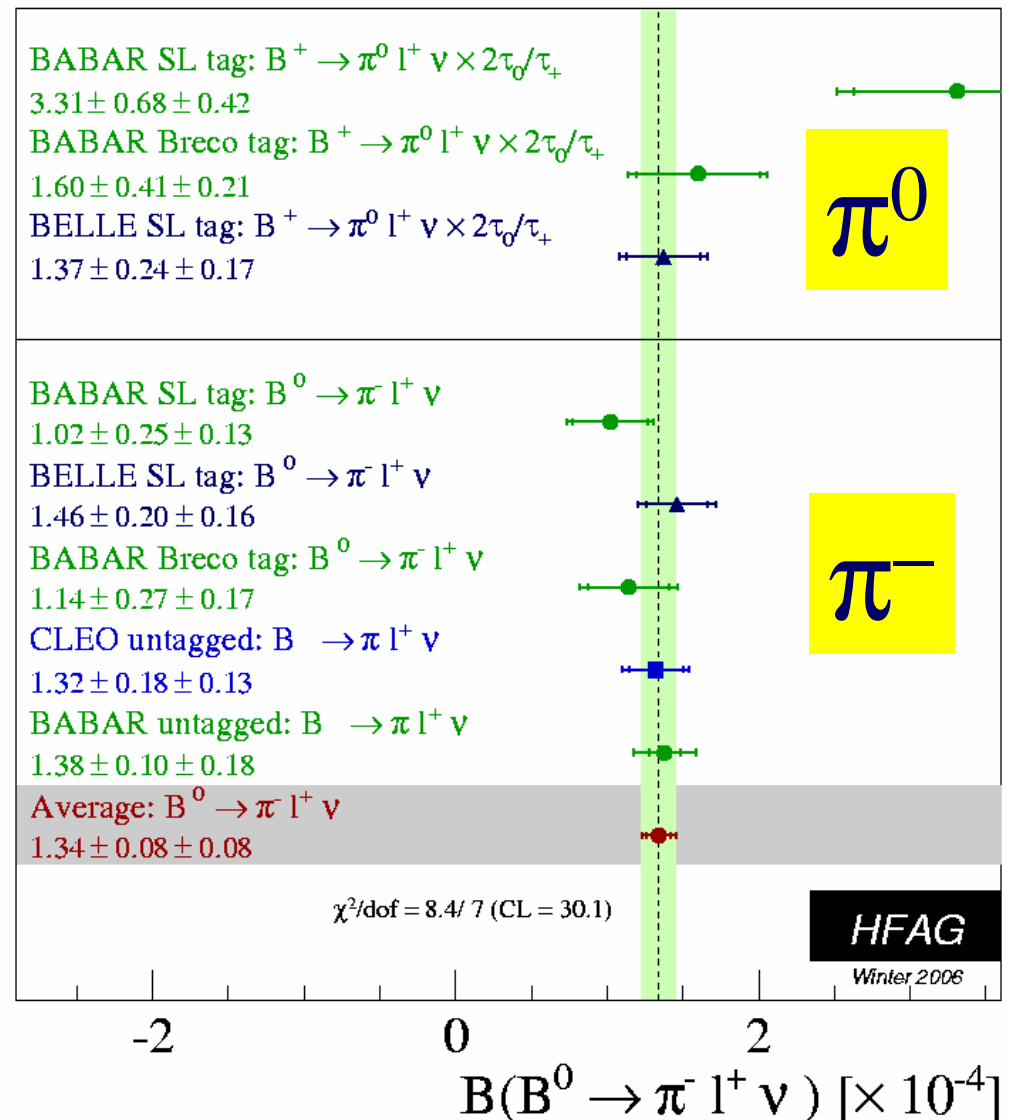
Summary of $B(B \rightarrow \pi \ell \nu)$ Exclusive

HFAG Winter 2006

Average $B(B^0 \rightarrow \pi^- l^+ \nu)$:
 $(1.34 \pm 0.08 \pm 0.08) \times 10^{-4}$

Note: Updated Belle SL tag result not yet incorporated in plot

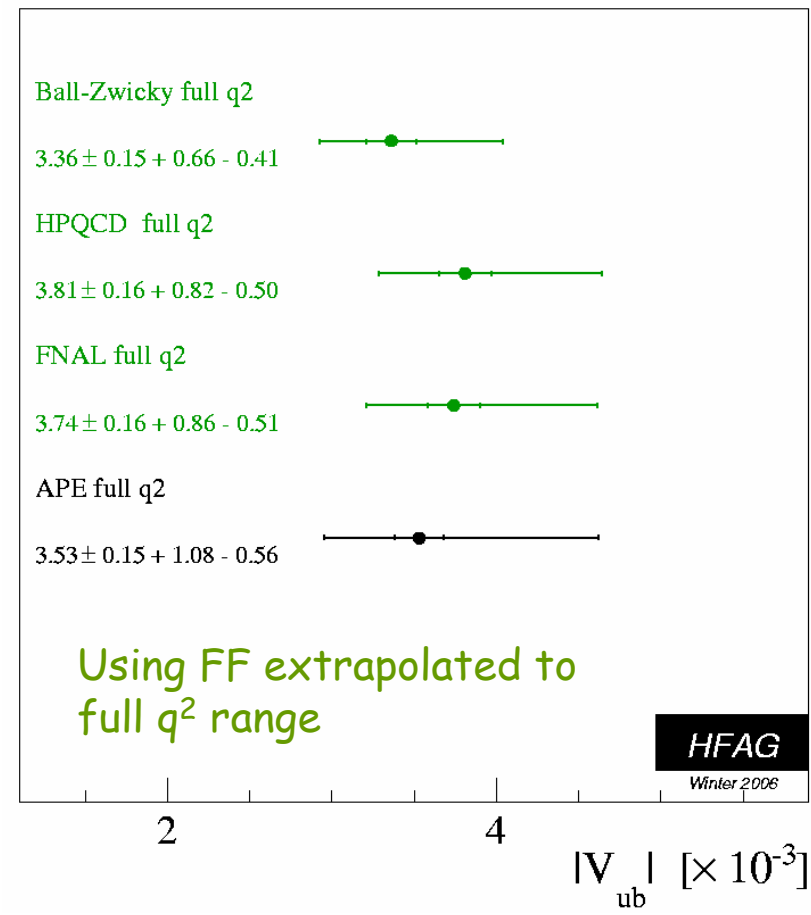
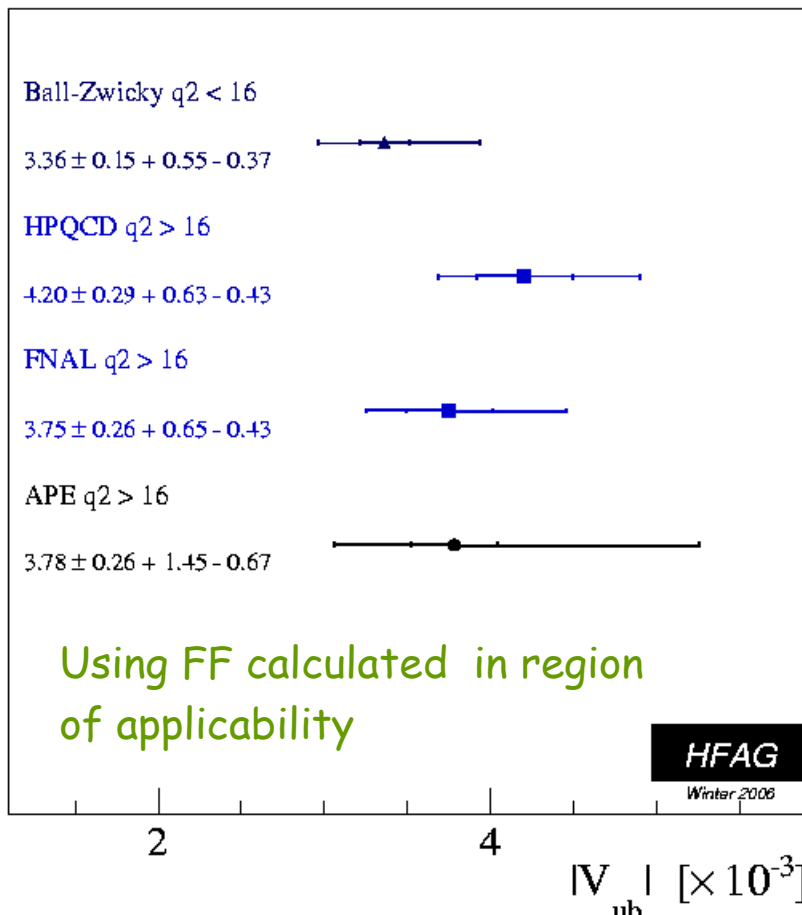
Untagged analyses currently the most precise



Summary of $|V_{ub}|$ from Exclusive $B \rightarrow \pi \ell \nu$

HFAG Winter 2006

Experimental q^2 shape input not used (yet)



Other $B \rightarrow X_u \ell \nu$ Exclusive Modes

Expt	Mode	Tag	BF [10^{-4}]	Reference
CLEO	$B^0 \rightarrow \rho^- \ell \nu$	Untagged	$2.17 \pm 0.34^{+0.47}_{-0.54} \pm 0.41$	PRD 68 (2003) 072003
CLEO	$B^0 \rightarrow \rho^- \ell \nu$	Untagged	$2.69 \pm 0.41^{+0.35}_{-0.47} \pm 0.50$	PRD 61 (2000) 052001
BaBar	$B^0 \rightarrow \rho^- \ell \nu$	Full	$2.57 \pm 0.52 \pm 0.59$	hep-ex/0408068
BaBar	$B^0 \rightarrow \rho^- e \nu$	Untagged	$3.29 \pm 0.42 \pm 0.47 \pm 0.60$	PRL 90 (2003) 181801
BaBar	$B^0 \rightarrow \rho^- \ell \nu$	Untagged	$2.14 \pm 0.21 \pm 0.51 \pm 0.28$	PRD 72 (2005) 051102
Belle	$B^0 \rightarrow \rho^- \ell \nu$	SL	$2.17 \pm 0.54 \pm 0.31 \pm 0.08$	hep-ex/0604024
CLEO	$B^+ \rightarrow \eta \ell \nu$	Untagged	$0.84 \pm 0.31 \pm 0.16 \pm 0.09$	PRD 68 (2003) 072003
Belle	$B^+ \rightarrow \rho^0 \ell \nu$	SL	$1.33 \pm 0.23 \pm 0.17 \pm 0.05$	hep-ex/06xxxxx
Belle	$B^+ \rightarrow \omega \ell \nu$	Untagged	$1.3 \pm 0.4 \pm 0.2 \pm 0.3$	PRL 93 (2004) 131803

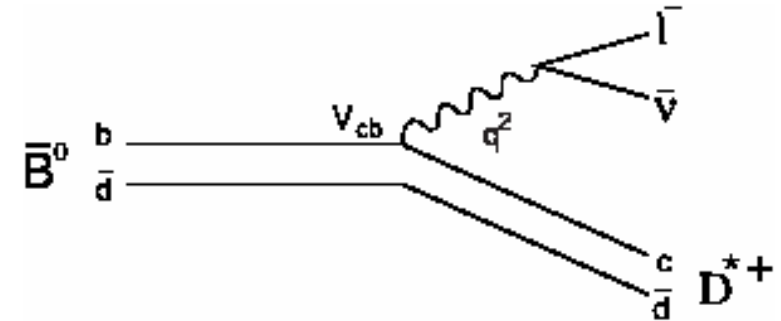
HFAG Compilation, except with updated Belle SL result included



BaBar Exclusive $|V_{cb}|$ Measurement

hep-ex/0602023

Update to
PRD 71 (2005) 051502
submitted to PRD

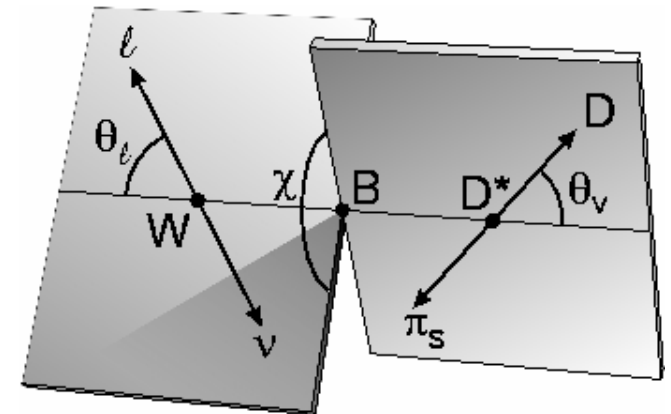


§ Multi-Dimensional fit to helicity amplitudes for ρ^2 (slope parameter) and R_1, R_2 (FF ratios), all functions of $H_{+,-,0}(w)$.

$$w = v_B \cdot v_{D^*}$$

$$\frac{d\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_V d\chi} = \frac{3G_F^2 |V_{cb}|^2 \rho_{D^*}^2 q^2}{8(4\pi)^4 M_B^2} \mathcal{B}_{D^*D} \times$$

$$\begin{aligned} & [H_+^2 (1 - \cos\theta_\ell)^2 \sin^2\theta_V + \\ & H_-^2 (1 + \cos\theta_\ell)^2 \sin^2\theta_V + \\ & 4H_0^2 \sin^2\theta_\ell \cos^2\theta_V \\ & - 2H_+ H_- \sin^2\theta_\ell \sin^2\theta_V \cos 2\chi \\ & - 4H_+ H_0 \sin\theta_\ell (1 - \cos\theta_\ell) \sin\theta_V \cos\theta_V \cos\chi \\ & + 4H_- H_0 \sin\theta_\ell (1 + \cos\theta_\ell) \sin\theta_V \cos\theta_V \cos\chi] \end{aligned}$$



79fb^{-1} (86M $B\bar{B}$)



BaBar Exclusive $|V_{cb}|$ Measurement (cont)

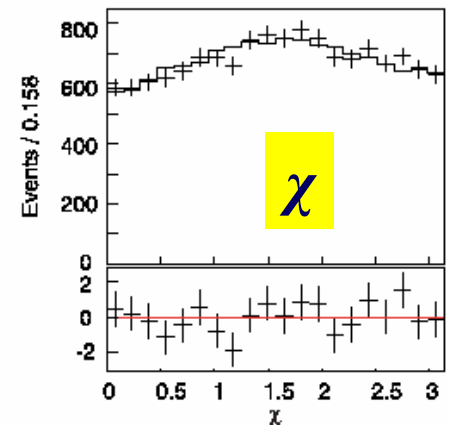
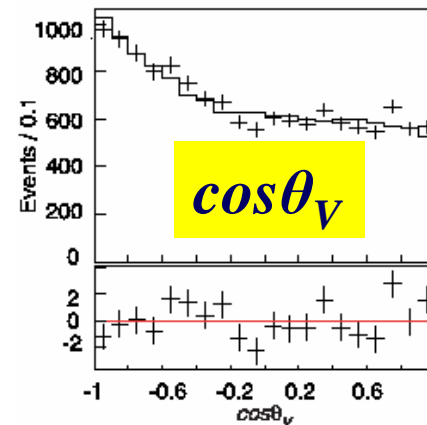
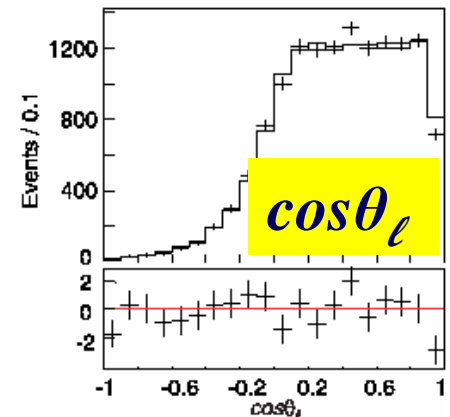
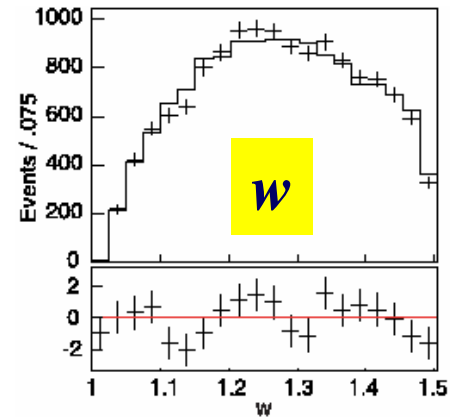
hep-ex/0602023

$$R_1 = 1.396 \pm 0.060 \pm 0.035 \pm 0.027$$

$$R_2 = 0.885 \pm 0.040 \pm 0.022 \pm 0.013$$

$$\rho^2 = 1.145 \pm 0.059 \pm 0.030 \pm 0.035$$

- Improvement in FF uncertainty
- Reduces $|V_{cb}|$ systematic error
- Useful for understanding $b \rightarrow c$ background in $b \rightarrow u$



$$|V_{cb}| = (37.6 \pm 0.3 \pm 1.3 \pm 1.5 \pm 1.3) \times 10^{-3}$$

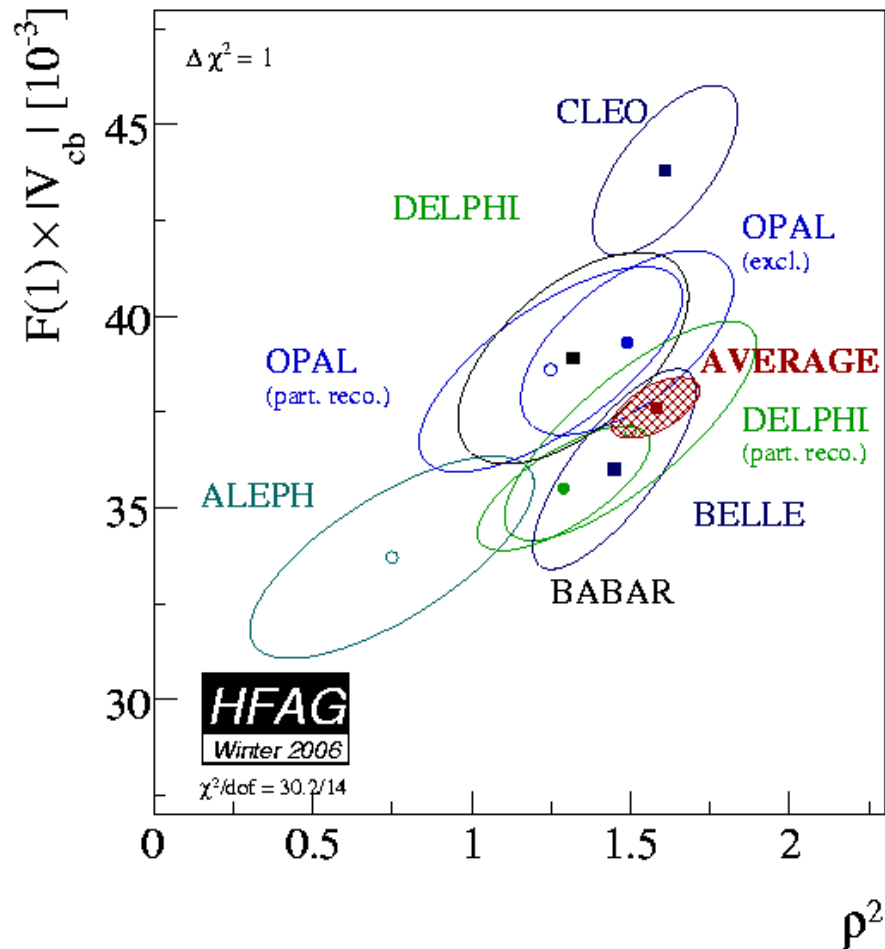
stat syst theo

Summary of Exclusive $|V_{cb}|$ Measurements

HFAG Winter 2006

Note:

Does not include latest
BaBar result from
hep-ex/0602023



Summary and Future : Exclusive $|V_{ub}|$ Measurements

§ CLEO, BaBar and Belle

⇒ X_u BF measurements using several channels and several techniques

$$X_u : \pi^+, \pi^0, \rho^+, \rho^0, \omega, \eta$$

⇒ $|V_{ub}|$ extracted using π^+, π^0 modes - Exptl error approaches 5%
- FF normalization error dominates

⇒ X_c BF measurements and $|V_{cb}|$ continue to be important

⇒ future precision X_u measurements using Full Recon tagging

⇒ FF shape measurements from experiment now possible

§ Theory progress important (and happening) as well (R. Hill talk)

(P. Mackenzie talk)

§ $|V_{ub}|$ to better than 5% precision overall from exclusive semileptonic B-factory measurements? ⇒ Feasible.